

**Second Semester M. Tech Degree Examination in  
Electronics and Communication Engineering  
Stream: Telecommunication Engineering (2013 Scheme)**

**TTE 2002 SECURE COMMUNICATION**

**MODEL QUESTION PAPER**

Time: 3 hours

Max. Marks: 60

Instructions: *Answer any 2 questions from each module (Each Carries 10 Marks)*

**Module I**

1. State and prove Fermat's little theorem.
2. Let  $p$  denote a prime, then prove that  $x^2 \equiv -1$  has solutions if and only if  $p=2$  or  $p \equiv 1 \pmod{4}$ .
3. Solve the congruences (i)  $x^3+2x-3 \equiv 0 \pmod{9}$  (ii)  $x^3+2x-3 \equiv 0 \pmod{5}$ .

**Module II**

4. Assume that two users want to establish a common secretkey over an insecure channel by using Diffie-Hellman key exchange protocol. The private key for user A is 11 and for user B is 14. Consider a commonly known prime 17.
  - (i) Find the smallest primitive element for  $p = 17$ .
  - (ii) Obtain the common key by using the primitive element found above.
5. Explain Data Encryption Standard.
6. Show that any sequence of positive integers  $\{v_i\}$  with  $v_{i+1} \geq 2v_i$  for all  $i$  is super increasing.

**Module III**

7. Find all bases  $b$  for which 15 is a pseudoprime.
8. Prove that 561 is the smallest Carmichael number.
9. Let  $n=4633$ . Find the smallest factor base  $B$  such that the squares of 68, 69 and 96 are  $B$  numbers and then factor 4633.